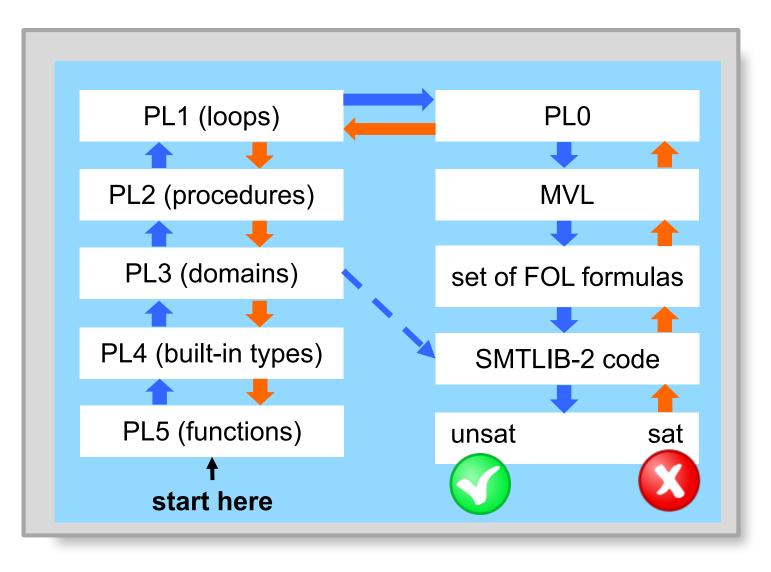
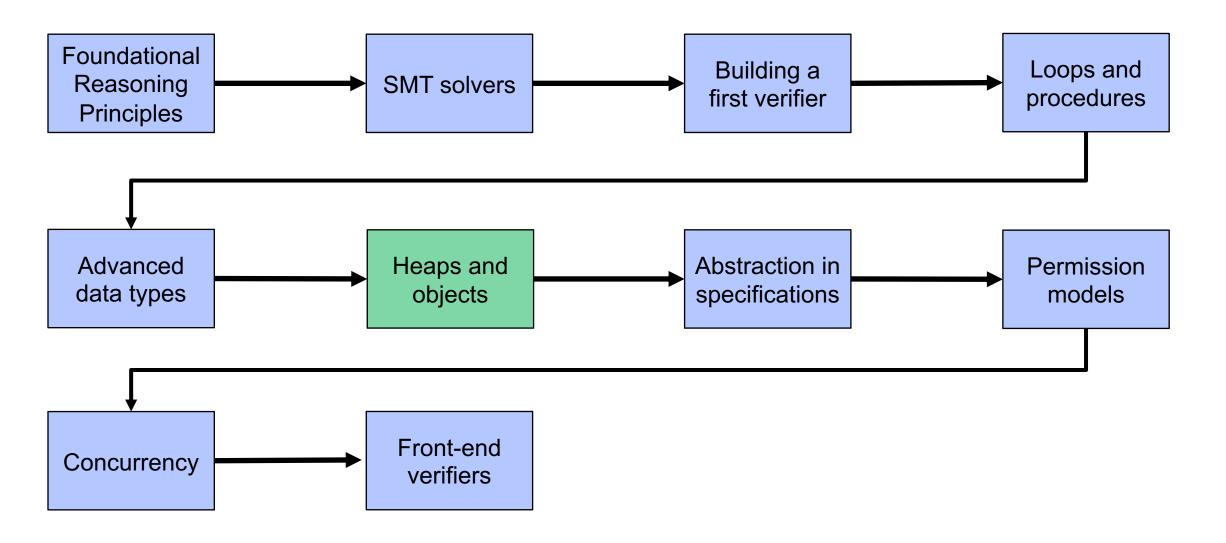
02245 – Module 7 **HEAPS AND OBJECTS**

Previously...



Tentative course outline



Why objects and heap-based data structures?

Static data structures

DTU

- Examples: arrays, all mathematical data structures from module 5
- Fixed size, stack-allocated
- Immutable, no memory reuse
- To update the data structure we create an updated copy

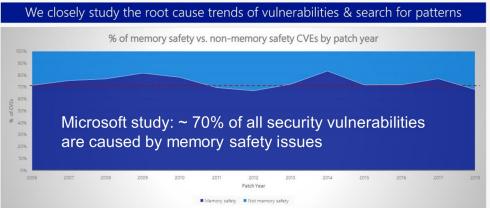
```
// static array A = [0,0,0]
A := cons(3, 0)
// create updated copy
B := set(A, 1, 17)
assert lookup(A, 1) == 0
```

- Dynamic data structures
 - Examples: resizable arrays, linked lists or trees, object graphs, ...
 - Dynamic size, heap-allocated
 - Mutable
 - To up update the data structure, we efficiently change it in-place

```
// dynamic array A = [0,0,0]
A := new Array(3, 0) // not Viper!
B := A // A, B reference same array
B[1] := 17 // in-place mutation
assert A[1] == 17
```

Why verification of heap-manipulating programs?

- Memory safety is the absence of errors related to memory accesses
 - dereferencing null-pointers
 - accessing unallocated (heap) memory
 - accessing dangling pointers
 - double-free bugs
 - use-after-free bugs



- Heap-manipulating programs are a prime target for program verification
 - Efficient algorithms need efficient data structures
 - Device drivers, embedded systems, ...
- Same concepts apply to concurrent programs

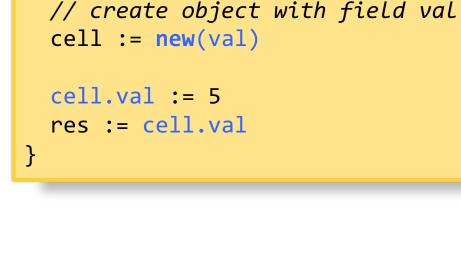
Objects and the heap

- 1. Heap model
- 2. Reasoning about objects and references
- 3. Ownership and access permissions
- 4. Encoding

Heap model: an object-based language

➔ 00-heap.vpr

- A heap is a set of objects
- No classes: each object can have all fields declared in the entire program
 - Type rules of a source language can be encoded
 - Memory consumption is not a concern since programs are not executed
- Objects are accessed via references
 - Field read and update operations
 - No information hiding
- No explicit de-allocation (garbage collector)
 - Conceptually, objects could remain allocated



var cell: Ref

field val: Int

method foo() returns (res: Int)

{

Extended programming language

Declarations D ::= field f: T	
Types T ::= Ref	
E ::= null E.f	
S ::= x := new(f) x := new(*) x.f := E	

(PL6)

Fields are declared globally

Only one type of references

Pre-defined null-reference Field read expression

Allocation with given fields or with all fields

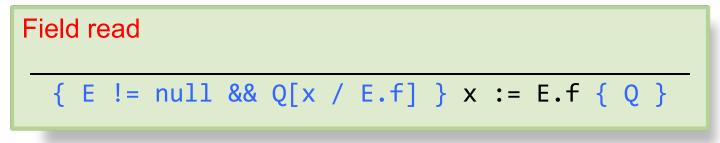
Field update of Ref-typed var.

Objects and the heap

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Proof rule for field read

Idea: treat field accesses like variable assignment

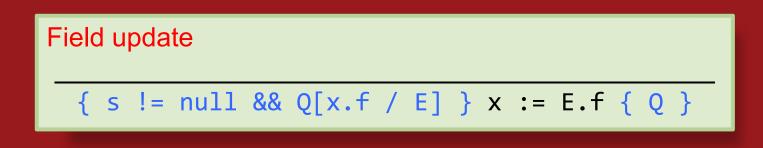


Additional well-definedness condition prevents null-dereferencing

```
{ true }
assume r != null && r.val == 5
{ r != null && r.val == 5 }
x := p.val
{ x == 5 }
assert x == 5
{ true }
```

Exercise: Naïve proof rule for field update

Idea: treat field accesses like variable assignment

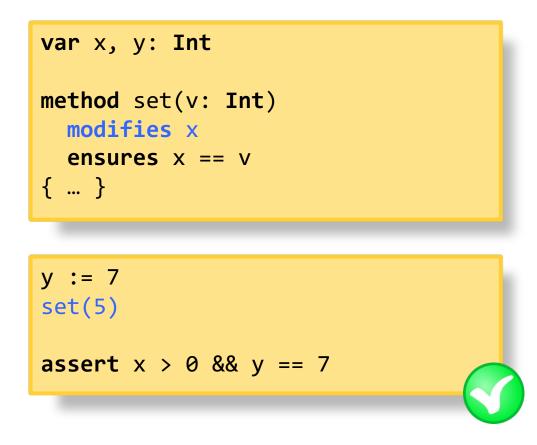


- Additional well-definedness condition prevents null-dereferencing
- The above rule for field update is *unsound*. Give an example that illustrates that.

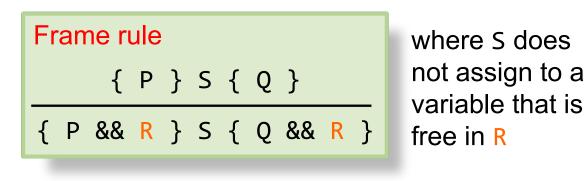


Reminder: method framing with global variables

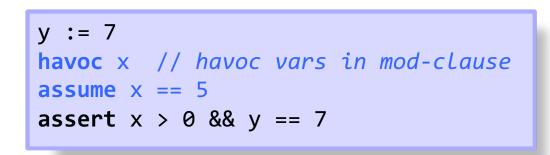
 Method specification declares which variables may get modified



Frame rule (for any statement S)



Encoding



Method framing with heap locations: modifies clause

 Idea: method specification declares which locations may get modified

```
method set(x: Ref, v: Int)
  modifies x.f
  ensures x.f == v
{ ... }
```

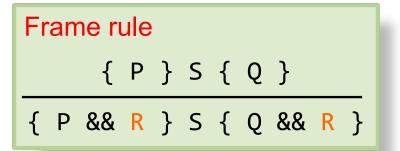


where S does not assign to a variable that is free in R

- Two ways to adapt the frame rule
 - «variable» means local or global variable, or «field»
 - «variable» means local or global variable, but not «field»

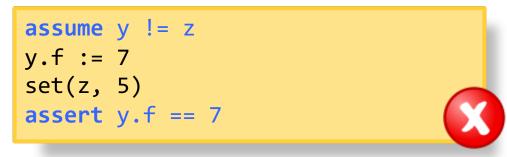
Method framing with heap locations: naïve approach

```
method set(x: Ref, v: Int)
  modifies x.f
  ensures x.f == v
{ ... }
```



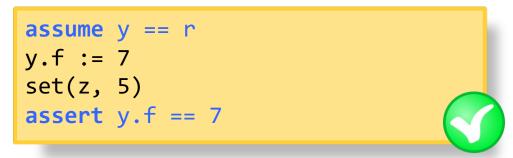
where S does not assign to a variable that is free in R

«variable» may mean «field»



 Incomplete: framing is very weak, as information about all objects is lost

«variable» does not mean «field»



 Unsound: this interpretation of the frame rule ignores aliasing!

Shortcomings of naïve method framing approach

- Sound encoding needs to consider aliasing
 - Inherits shortcomings of candidate rule for field updates
 - Explosion of cases
 - Treatment of assertions that depend on heap locations implicitly

```
y.f := 7
// encoding of set(z, 5)
var tmp: Int
z.f := tmp // considers aliasing
assume z.f == 5
assert y.f == 7
```

- Many methods modify a statically-unknown set of heap locations
 - Locations cannot be listed explicitly in a modifies clause

```
method sort(list: Ref)
   modifies list.val, list.next.val, list.next.val, ...
{ ... }
```

Listing modified heap locations violates information hiding

Summary of challenges

Heap data structures pose three major challenges for sequential verification

- Reasoning about aliasing
- Framing, especially for dynamic data structures
- Writing specifications that preserve information hiding

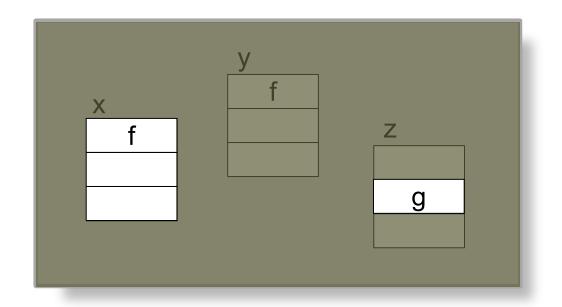
Additional challenges for concurrent programs, e.g., data races

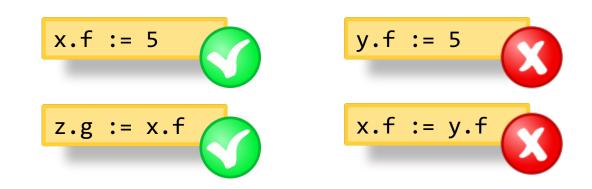
Objects and the heap

- 1. Heap model
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- 4. Encoding

Access permissions

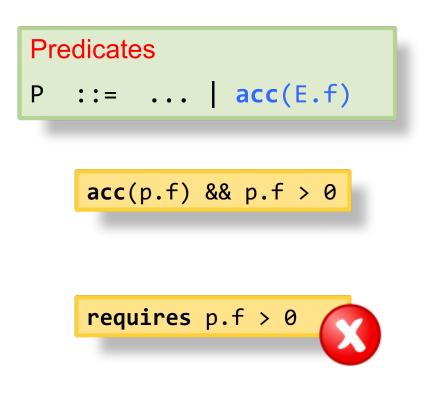
- Associate each heap location with at most one permission
- Read or write access to a memory location requires permission
- Permissions are created when the heap location is allocated
- Permissions can be transferred, but not duplicated or forged





Permission assertions

- Permissions are denoted by access predicates
 - Access predicates are *not* permitted under negations, disjunctions, and on the left of implications
- Predicates may contain both permissions and value constraints
- Predicates must be self-framing, that is, include all permissions to evaluate their heap accesses
- An assertion that does not contain access predicates is called pure or heap independent





Exercise: swapping the fields of two objects

- Implement a swap method that exchanges the field values of two objects.
- Specify its functional behavior.
- Write a client method that creates two objects and calls swap on them. Include an assertion to check that swap's specification is strong enough.
- Change your client method such that it calls swap, passing the same reference twice.

field f: Int
<pre>method swap(a: Ref, b: Ref) { }</pre>

04-swap.vpr



Permission assertions and aliasing

Reminder:

- There is at most one permission for every heap location
- Permissions can be transferred, but not duplicated or forged

If we have two permissions acc(a.f) and acc(b.f), can a and b be aliases?

```
field f: Int
method alias(a: Ref, b: Ref)
  requires acc(a.f) && acc(b.f)
{
    a.f := 5
    b.f := 7
    assert a.f == 5
}
```

```
field f: Int
method alias2(a: Ref, b: Ref)
requires acc(a.f) && acc(b.f)
{
  assert a == b
  }
  How do we justify this?
```

Permission assertions, more formally

- We extend states to stack-heap pairs $\sigma = (s, h)$
- The stack $s: Var \rightarrow Value$ assigns values to variables
 - We used this as the full state state used in all previous classes
- The heap h assigns values to object-field pairs
 h: Objects × Fields finite partial
 Value
 - dom(h) is the set of all object-field pairs for which h is defined
 - $(obj, f) \in dom(h)$ means we have permission to field f of object obj

Predicates over extended states

$\Im = (\mathfrak{A}, s, h) \models P$ if and only if
$(\Im(t), f) \in dom(h)$
$\Im(t_1) = \Im(t_2)$
$\left(\mathfrak{I}(t_1),\ldots,\mathfrak{I}(t_n)\right)\in R^{\mathfrak{A}}$
$\mathfrak{T} \models \mathbf{Q} \text{ and } \mathfrak{T} \models \mathbf{R}$
If $\mathfrak{I} \models \mathbf{Q}$, then $\mathfrak{I} \models \mathbf{R}$
For some $v \in \mathbf{T}^{\mathfrak{A}}$, $\mathfrak{I}[x := v] \models \mathbf{Q}$
For all $v \in \mathbf{T}^{\mathfrak{A}}$, $\mathfrak{I}[x \coloneqq v] \models \mathbf{Q}$

Self-framing predicates are always well-defined

Assume s(a) == s(b) and h(a.f) == s(c)

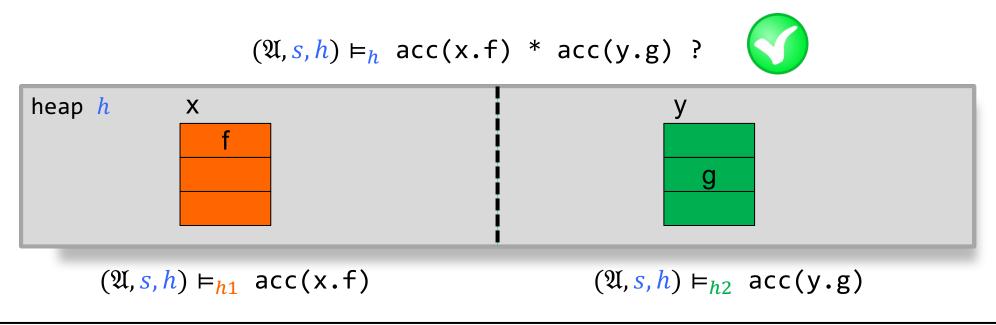
Does $\Im = (\mathfrak{A}, \underline{s}, \underline{h}) \vDash \operatorname{acc}(a.f) \land \operatorname{acc}(b.f) \ b.f == c \ hold?$

 $\Im(t)$ is the value obtained from evaluating term *t* in interpretation \Im

Examples: $\Im(x) = s(x)$ $\Im(x + 17) = s(x) + \mathfrak{A} 17^{\mathfrak{A}}$ $\Im(x.f) = h(s(x), f)$ $\Im(x.f.g) = h(h(s(x), f), g)$

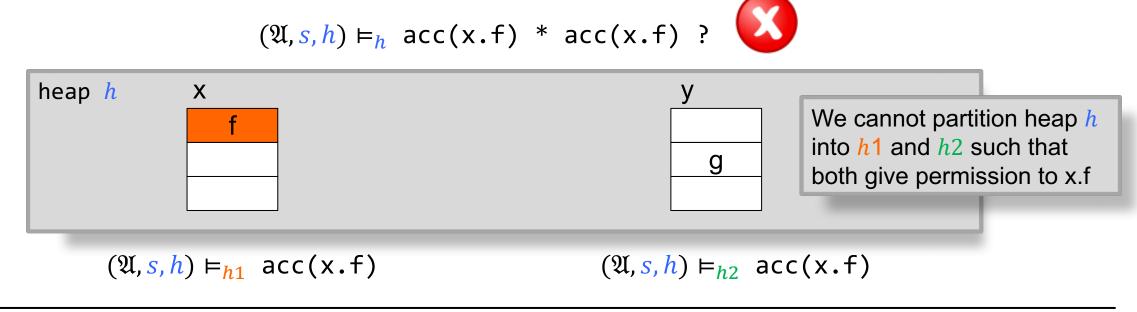
Handling aliasing

- Problem: having permissions a.f and b.f should mean a and b are no aliases
- We introduce a new connective: the separating conjunction P * Q
 - P * Q partitions the heap *h* into two chunks
 - Every permission assertion acc(E.f) is evaluated in its own heap chunk
 - All other predictes are evaluated in the full heap



Handling aliasing

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 - All other predictes are evaluated in the full heap



Predicates with separating conjunction

Predicate P	$\mathfrak{I} = (\mathfrak{A}, s, h) \vDash_{h'} P$ if and only if		
<pre>acc(t.f)</pre>	$(\mathfrak{I}(t), f) \in dom(h')$	evaluate access permissions in current heap chunk h' (initially h)	
$t_1 = t_2$	$\Im(t_1) = \Im(t_2)$		
$R(t_1, \dots, t_n)$	$(\Im(t_1), \dots, \Im(t_n)) \in R^{\mathfrak{A}}$		
$\mathbf{Q} \wedge \mathbf{R}$	$\mathfrak{I} \vDash_{h'} \mathbf{Q}$ and $\mathfrak{I} \vDash_{h'} \mathbf{R}$		
Q * R	exists partition of h' into $h1$, $h2$ such that	split current heap chunk into two	
	$\mathfrak{I} \vDash_{h1} \mathbf{Q} \text{ and } \mathfrak{I} \vDash_{h2} \mathbf{R}$		

- $\mathbf{Q} * \mathbf{R}$ and $\mathbf{Q} \wedge \mathbf{R}$ are equivalent if \mathbf{Q} and \mathbf{R} are pure
- Holding permission to x.f and y.f implies that x and y are no aliases

acc(x.f) * acc(y.f) ==> x != y



Separating Conjunction in Viper

- Viper's && is the separating conjunction *
- Viper has no ordinary conjunction ∧
- Q * R and Q ^ R are equivalent if Q and R are pure (heap independent)
- For the call swap(x, x), the precondition is equivalent to false

method swap(a: Ref, b: Ref)
 requires acc(a.f) && acc(b.f)

→ 04-swap.vpr
→ 05-alias.vpr

Exercise

DTU

Reconsider the method on the right.

 Change the precondition such that we can call the method by passing both aliasing references and non-aliasing references to it as arguments without violating the precondition.

```
method alias(a: Ref, b: Ref)
    requires acc(a.f) && acc(b.f)
{
    a.f := 5
    b.f := 7
    assert a.f == 5
}
```

 Does the assertion still hold? Why (not)?

Challenges revisited

Heap data structures pose three major challenges for sequential verification

- Reasoning about aliasing
 - Permissions and separating conjunction



Writing specifications that preserve information hiding

And additional challenges for concurrent programs, e.g., data races



Field access: proof rules with permissions

- Each field access requires (and preserves) the corresponding permission
- Permission to a location implies that the receiver is non-null
- Substitution with logical variable N in the field-update rule is needed to handle occurrences of x.f inside E (e.g., x.f := x.f + 1)

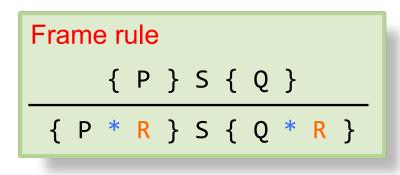
Framing

Frame rule
{ P } S { Q }
{ P ^ R } S { Q ^ R }

where S does not assign to a variable that is free in R

Unsound if S assigns to heap locations constrained by R

Framing



where S does not assign to a variable that is free in R

- The frame R must be self-framing
 - If heap locations constrained by R are disjoint from those modified by S, R is preserved
 - Otherwise, the precondition is equivalent to false (the triple holds trivially)
- Example

{ acc(x.f) * x.f = N } x.f := 5 { acc(x.f) * x.f = 5 }

 $\{ acc(x.f) * x.f = N * acc(y.f) * y.f = 7 \} x.f := 5 \{ acc(x.f) * x.f = 5 * acc(y.f) * y.f = 7 \}$

Framing (cont'd)

• The following proof derives an incorrect triple. Why is it not a valid proof?

$$\{ acc(x.f) * x.f = N \} x.f := 5 \{ acc(x.f) * x.f = 5 \}$$

{
$$acc(x.f) * x.f = N * x.f = 1$$
 } $x.f := 5$ { $acc(x.f) * x.f = 5 * x.f = 1$ }

- Recall that the frame must be self-framing, which is not the case here
- Making the frame self-framing yields a valid (but vacuous) proof

 $\label{eq:started_st$

Framing for method calls

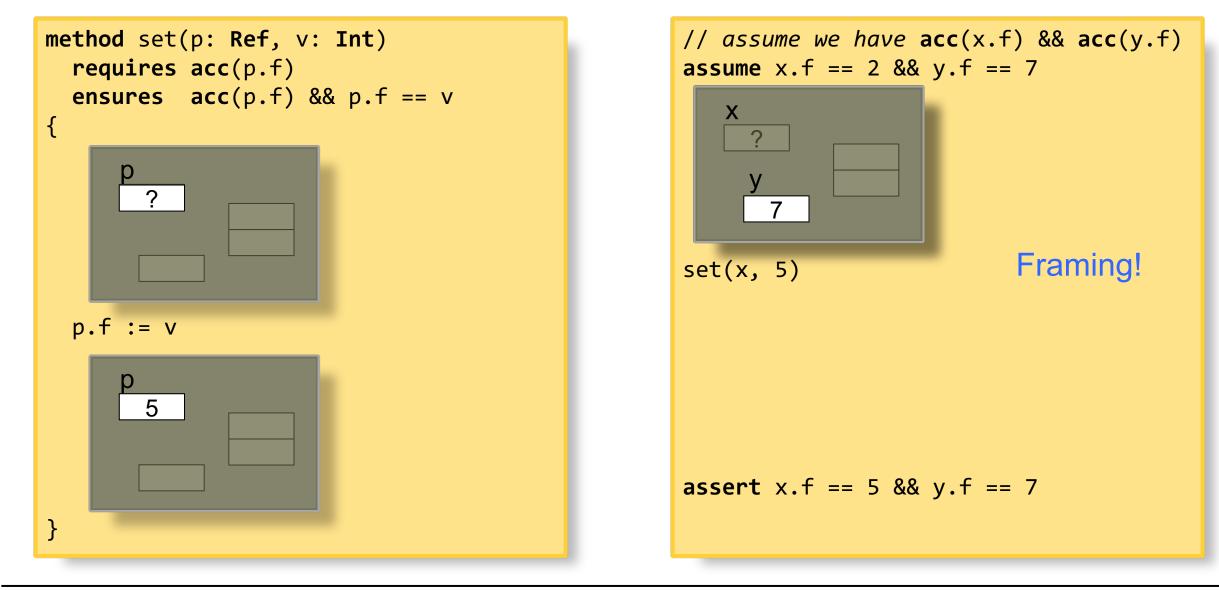
```
method set(p: Ref, v: Int)
  requires acc(p.f)
  ensures acc(p.f) && p.f == v
{
   p.f := v
}
```

```
// assume we have acc(x.f) && acc(y.f)
assume y.f == 7
set(x, 5)
assert x.f == 5 && y.f == 7
```

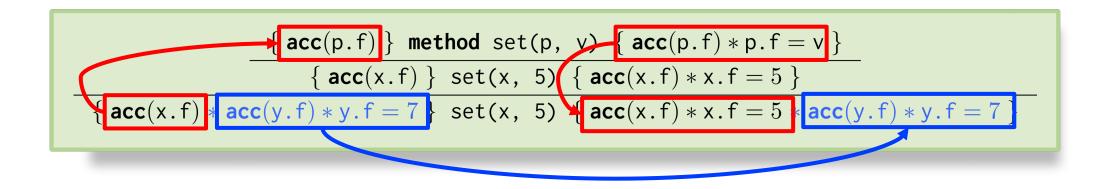
$$\label{eq:constraint} \begin{array}{c} \left\{ \mbox{ acc}(p.f) \right\} \mbox{ method } set(p, \ v) \ \left\{ \mbox{ acc}(p.f) * p.f = v \right\} \\ \hline \left\{ \mbox{ acc}(x.f) \right\} \ set(x, \ 5) \ \left\{ \mbox{ acc}(x.f) * x.f = 5 \right\} \\ \left\{ \mbox{ acc}(y.f) * y.f = 7 \right\} \ set(x, \ 5) \ \left\{ \mbox{ acc}(x.f) * x.f = 5 * \mbox{ acc}(y.f) * y.f = 7 \right\} \end{array}$$

- Frame rule enables framing without modifies clauses
- A method may modify only heap locations to which it has permission

Permission transfer



Permission transfer for method calls

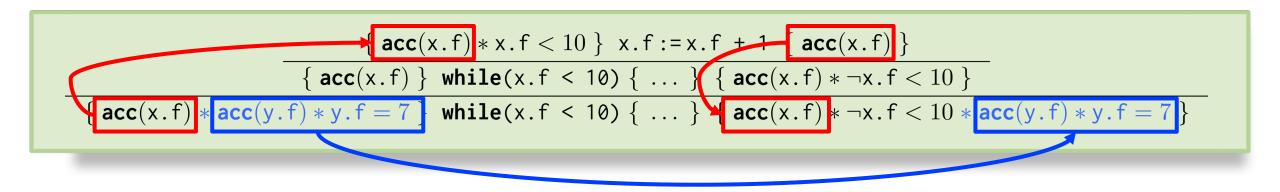


- Permissions are held by method executions or loop iterations
- Calling a method transfers permissions from the caller to the callee (according to the method precondition)
- Returning from a method transfers permissions from the callee to the caller (according to the method postcondition)
- Residual permissions are framed around the call

Framing for loops

```
// assume we have acc(x.f) && acc(y.f)
x.f := 0
y.f := 7
while (x.f < 10)
    invariant acc(x.f)
{
    x.f := x.f + 1
}
assert y.f == 7</pre>
```

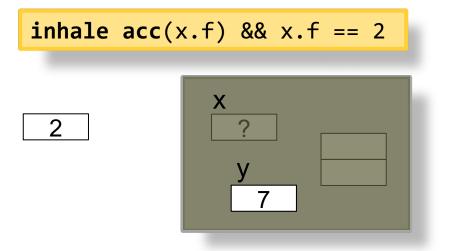
Permission transfer for loops



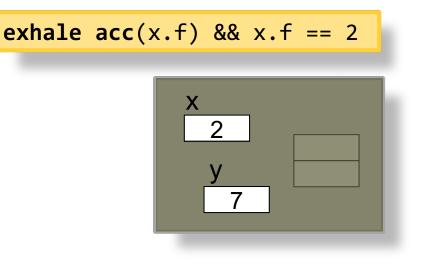
- Permissions are held by method executions or loop iterations
- Entering a loop transfers permissions from the enclosing context to the loop (according to the loop invariant)
- Leaving a loop transfers permissions from the loop to the enclosing context (according to the loop invariant)
- Residual permissions are framed around the loop

Permission transfer: inhale and exhale operations

- inhale P means:
 - obtain all permissions required by assertion P
 - assume all logical constraints



- exhale P means:
 - assert all logical constraints
 - check and remove all permissions required by assertion P
 - havoc any locations to which all permission is lost





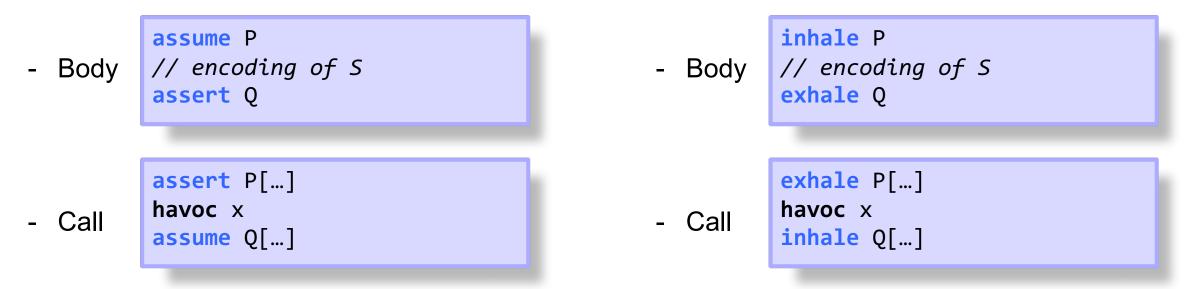
Encoding of method bodies and calls

```
method foo() returns (...)
   requires P
   ensures Q
{ S }
```

x := foo()

Encoding with heap

Encoding without heap and globals

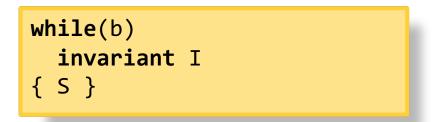


inhale and exhale are permission-aware analogues of assume and assert

Exercise: definition of exhale

- exhale P means:
 - assert all logical constraints
 - check and remove all permissions required by P
 - havoc (reset) any locations to which all permission is lost
- Write an example that demonstrates that omitting the havoc from the exhale encoding would be unsound

Encoding of loops



Reminder: encoding without heap

```
assert I
havoc targets
assume I
if(*) {
   assume b
   // encoding of S
   assert I
   assume false
} else {
   assume !b
}
```

Encoding with heap

```
exhale I
havoc targets
inhale I
if(*) {
   assume b
   // encoding of S
   exhale I
   assume false
} else {
   assume !b
}
```

Encoding of allocation

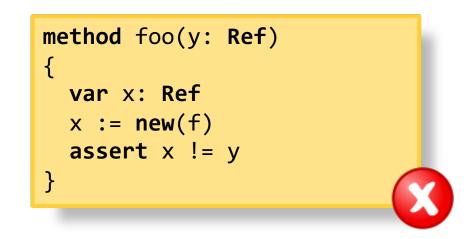
 new-expression specifies the relevant fields

x := **new**(f, g)

 Encoding chooses an arbitrary reference and inhales permissions to relevant fields

```
var x: Ref
inhale acc(x.f) && acc(x.g)
```

 Incomplete information about freshness of new object



Exercise: working with permissions

- Implement, specify, and verify a class for bank accounts with the following methods:
 - create returns a fresh account with initial balance 0
 - deposit deposits a non-negative amount to an account
 - transfer transfers a non-negative amount between two accounts
 - Account balances are integers.

Verify the client program on the right.

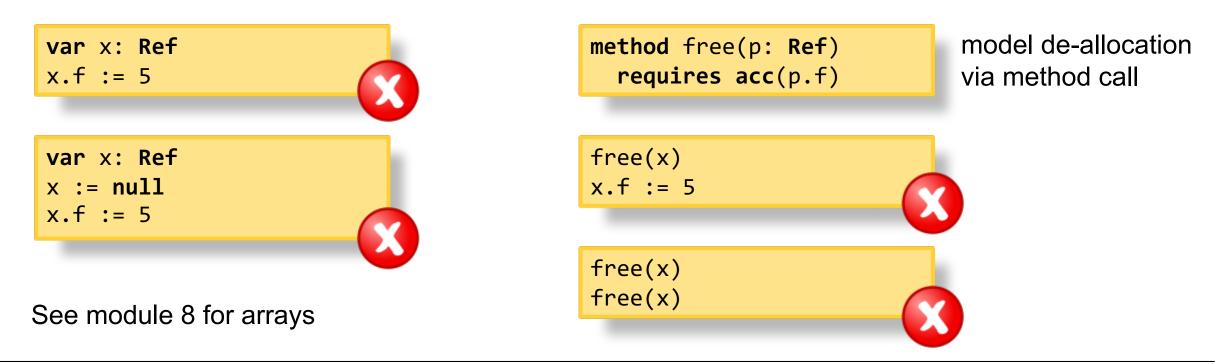
```
→ 07-account.vpr
```

<pre>method client()</pre>
{
var x: Ref
var y: Ref
var z: Ref
x := create()
y := create()
z := create()
deposit(x, 100)
deposit(y, 200)
deposit(z, 300)
transfer(x, y, 100)
assert x.bal == 0
assert y.bal == 300
assert z.bal == 300
}



Verifying memory safety

- Memory safety is the absence of errors related to memory accesses, such as, null-pointer dereferencing, access to un-allocated memory, dangling pointers, outof-bounds accesses, double free, etc.
- Using permissions, Viper verifies memory safety by default



Challenges revisited

Heap data structures pose three major challenges for sequential verification

- Reasoning about aliasing
 - Permissions and separating conjunction
- Framing, especially for dynamic data structures
 - Sound frame rule, but no support yet for unbounded data structures



Writing specifications that preserve information hiding

And additional challenges for concurrent programs, e.g., data races



Objects and the heap

- 1. Heap model
- 2. Reasoning about objects and references
- 3. Ownership and access permissions
- 4. Encoding

Heaps

Encode references and fields

type Ref const null: Ref	// type for references // null references
type Field T	<pre>// polymorphic type for field names</pre>
field f: Int field g: Ref	<pre>const f: Field int const g: Field Ref</pre>

Heaps map references and field names to values

type HeapType = Map<T>[(Ref, Field T), T] // polymorphic map

Represent the program heap as one global variable

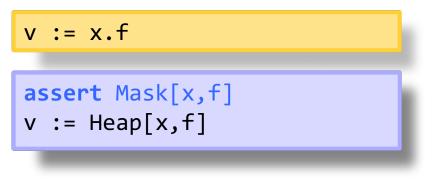
var Heap: HeapType

Permissions and field access

Permissions are tracked in a global permission mask

```
type MaskType = Map<T>[(Ref, Field T), bool]
var Mask: MaskType
```

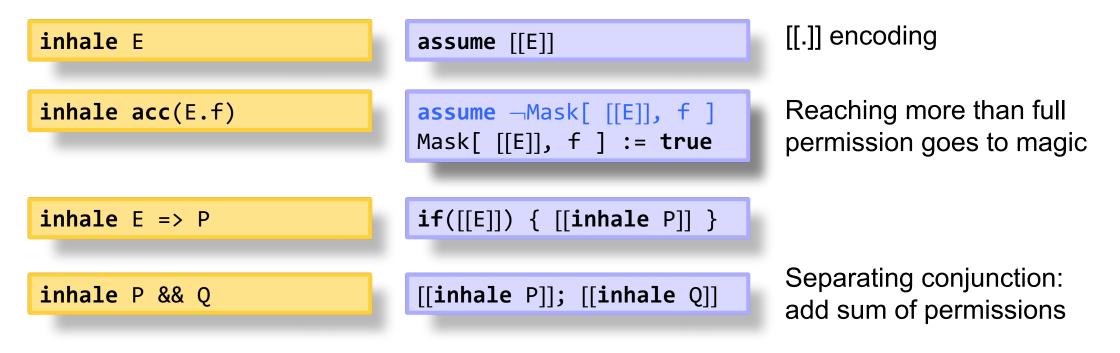
- Convention: ¬Mask[null, f] for all fields f
- Field access



- Field access requires permission!

Inhale

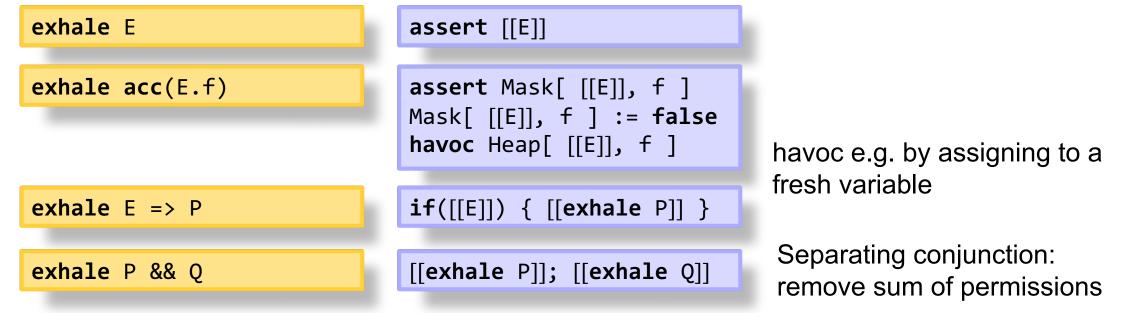
- **inhale** P means:
 - obtain all permissions required by assertion P
 - assume all logical constraints
- Encoding is defined recursively over the structure of P



The encoding also asserts that E is well-defined (omitted here)

Exhale (1st attempt)

- exhale P means:
 - assert all logical constraints
 - check and remove all permissions required by assertion P
 - havoc any locations to which all permission is lost
- Encoding is defined recursively over the structure of P



The encoding also asserts that E is well-defined (omitted here)

Example

inhale acc(x.f) && x.f == 5

assume -Mask[x,f]
Mask[x,f] := true

assert Mask[x,f] // well-definedness check
assume Heap[x,f] == 5

exhale acc(x.f) && x.f == 5

assert Mask[x,f] Mask[x,f] := false havoc Heap[x,f] assert Mask[x,f] // well-definedness check assert Heap[x,f] == 5

Exhale (fixed)

- Conceptually, permissions should be removed after checking logical constraints
- Adapt encoding
 - Check well-definedness against mask at the beginning of the exhale
 - Delay havoc until the end of the exhale

```
exhale P
```

Exercise: encoding of exhale

Encode the operation

```
exhale acc(x.f) && x.f == 5
```

with the fixed encoding.

Challenges revisited

Heap data structures pose three major challenges for sequential verification

- Reasoning about aliasing
 - Permissions and separating conjunction
- Framing, especially for dynamic data structures
 - Sound frame rule, but no support yet for unbounded data structures
- Writing specifications that preserve information hiding
 - Not solved, but see next module

And additional challenges for concurrent programs, e.g., data races

- Permissions are an excellent basis, but see later



