02245 – Module 7

HEAPS AND OBJECTS

Previously...

Tentative course outline

Why objects and heap-based data structures?

- Static data structures
	- Examples: arrays, all mathematical data structures from module 5
	- Fixed size, stack-allocated
	- Immutable, no memory reuse
	- To update the data structure we create an updated copy

```
// static array A = [0,0,0]A := \text{cons}(3, 0)// create updated copy
B := set(A, 1, 17)assert lookup(A, 1) == 0
```
- Dynamic data structures
	- Examples: resizable arrays, linked lists or trees, object graphs, ...
	- Dynamic size, heap-allocated
	- Mutable
	- To up update the data structure, we efficiently change it in-place

```
// dynamic array A = [0,0,0]
A := new Array(3, 0) // not Viper!
B := A / / A, B reference same array
B[1] := 17 // in-place mutation
assert A[1] == 17
```
Why verification of heap-manipulating programs?

- Memory safety is the absence of errors related to memory accesses
	- dereferencing null-pointers
	- accessing unallocated (heap) memory
	- accessing dangling pointers
	- double-free bugs
	- use-after-free bugs

- § Heap-manipulating programs are a prime target for program verification
	- Efficient algorithms need efficient data structures
	- Device drivers, embedded systems, ...
- § Same concepts apply to concurrent programs

Objects and the heap

- 1. Heap model
- 2. Reasoning about objects and references
- 3. Ownership and access permissions
- 4. Encoding

Heap model: an object-based language \rightarrow 00-heap.vpr

- A heap is a set of objects
- No classes: each object can have all fields declared in the entire program
	- Type rules of a source language can be encoded
	- Memory consumption is not a concern since programs are not executed
- Objects are accessed via references
	- Field read and update operations
	- No information hiding
- No explicit de-allocation (garbage collector)
	- Conceptually, objects could remain allocated

res := cell.val

field val: **Int**

}

Extended programming language (PL6)

III

Declarations D ::= ... | **field** f: T Expressions E ::= ... | **null** | E.f Statements S ::= ... | x := **new**(f!) | x := **new**(*) | x.f := E Types T ::= ... | **Ref** Allocation with given fields Field update of **Ref**-typed var. Only one type of references Pre-defined null-reference Field read expression Fields are declared globally

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or with all fields

Objects and the heap

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Proof rule for field read \rightarrow 01-field-read.vpr

■ Idea: treat field accesses like variable assignment

■ Additional well-definedness condition prevents null-dereferencing

Exercise: Naïve proof rule for field update

■ Idea: treat field accesses like variable assignment

- Additional well-definedness condition prevents null-dereferencing
- The above rule for field update is *unsound*. Give an example that illustrates that.

Reminder: method framing with global variables

■ Method specification declares which variables may get modified

■ Frame rule (for any statement S)

■ Encoding

Method framing with heap locations: modifies clause

■ Idea: method specification declares which locations may get modified

where S does not assign to a variable that is free in R

- § Two ways to adapt the frame rule
	- «variable» means local or global variable, or «field»
	- «variable» means local or global variable, but not «field»

Method framing with heap locations: naïve approach

```
method set(x: Ref, v: Int)
  modifies x.f
  ensures x.f == v
{ … }
```


where S does not assign to a variable that is free in R

«variable» may mean «field»

■ Incomplete: framing is very weak, as information about all objects is lost

«variable» does not mean «field»

■ Unsound: this interpretation of the frame rule ignores aliasing!

Shortcomings of naïve method framing approach

- Sound encoding needs to consider aliasing
	- Inherits shortcomings of candidate rule for field updates
	- Explosion of cases
	- Treatment of assertions that depend on heap locations implicitly

```
y.f := 7// encoding of set(z, 5)
var tmp: Int
z.f := tmp // considers aliasing
assume z.f == 5
assert y.f == 7
```
- Many methods modify a statically-unknown set of heap locations
	- Locations cannot be listed explicitly in a modifies clause

```
method sort(list: Ref)
  modifies list.val, list.next.val, list.next.next.val, …
{ … }
```
■ Listing modified heap locations violates information hiding

Summary of challenges

Heap data structures pose three major challenges for sequential verification

- Reasoning about aliasing
- Framing, especially for dynamic data structures
- Writing specifications that preserve information hiding

Additional challenges for concurrent programs, e.g., data races

Objects and the heap

- 1. Heap model
- 2. Reasoning about objects and references
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Access permissions

- § Associate each heap location with *at most one* permission
- Read or write access to a memory location requires permission
- Permissions are created when the heap location is allocated
- Permissions can be transferred, but not duplicated or forged

Permission assertions \rightarrow 03-object.vpr

- Permissions are denoted by access predicates
	- Access predicates are *not* permitted under negations, disjunctions, and on the left of implications
- Predicates may contain both permissions and value constraints
- Predicates must be self-framing, that is, include all permissions to evaluate their heap accesses
- An assertion that does not contain access predicates is called pure or heap independent

Exercise: swapping the fields of two objects

- Implement a swap method that exchanges the field values of two objects.
- Specify its functional behavior.
- Write a client method that creates two objects and calls swap on them. Include an assertion to check that swap's specification is strong enough.
- Change your client method such that it calls swap, passing the same reference twice.

è 04-swap.vpr

Permission assertions and aliasing \rightarrow **05-alias.vpr**

Reminder:

- There is a*t most one* permission for every heap location
- Permissions can be transferred, but not duplicated or forged

If we have two permissions $acc(a.f)$ and $acc(b.f)$, can a and b be aliases?

```
field f: Int
method alias(a: Ref, b: Ref)
  requires acc(a.f) && acc(b.f)
{
 a.f := 5b.f := 7assert a.f == 5
}
```

```
field f: Int
method alias2(a: Ref, b: Ref)
  requires acc(a.f) && acc(b.f)
{
  assert a == b
}
    \rightarrow How do we justify this?
```
Permission assertions, more formally

- We extend states to stack-heap pairs $\sigma = (s, h)$
- **The stack s: Var** \rightarrow **Value assigns values to variables**
	- We used this as the full state state used in all previous classes
- **The heap h assigns values to object-field pairs** *h*: Objects×Fields $\xrightarrow{\text{finite partial}}$ Value
	- $dom(h)$ is the set of all object-field pairs for which h is defined
	- (obj, f) $\in dom(h)$ means we have permission to field f of object obj

Predicates over extended states

■ Self-framing predicates are always well-defined

Assume $s(a) == s(b)$ and $h(a.f) == s(c)$

Does $\mathfrak{I} = (\mathfrak{A}, s, h) \vDash acc(a.f) \land acc(b.f) b.f == c hold?$

 $\Im(t)$ is the value obtained from evaluating term t in interpretation $\mathfrak I$

Examples: $\Im(x) = s(x)$ $\Im(x + 17) = s(x) + 17^{\mathfrak{A}}$ $\mathfrak{I}(x,f) = h(s(x),f)$ $\Im(x, f, g) = h(h(s(x), f), g)$

Handling aliasing

- Problem: having permissions a.f and b.f should mean a and b are no aliases
- We introduce a new connective: the separating conjunction P $* Q$
	- $P * Q$ partitions the heap h into two chunks
	- Every permission assertion acc(E.f) is evaluated in its own heap chunk
	- All other predictes are evaluated in the full heap

Handling aliasing

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Predicates with separating conjunction

- § **Q** ∗ **R** and **Q** ∧ **R** are equivalent if **Q** and **R** are pure
- \blacksquare Holding permission to x.f and y.f implies that x and y are no aliases

 $\textsf{acc}(x.f) * \textsf{acc}(y.f) ==> x != y$

Separating Conjunction in Viper

- Viper's && is the separating conjunction $*$
- Viper has no ordinary conjunction \wedge
- § **Q** ∗ **R** and **Q** ∧ **R** are equivalent if **Q** and **R** are pure (heap independent)
- For the call swap(x, x), the precondition is equivalent to false

method swap(a: **Ref**, b: **Ref**) **requires acc**(a.f) && **acc**(b.f)

 \rightarrow 04-swap.vpr \rightarrow 05-alias.vpr

Exercise

DTU

■ Reconsider the method on the right.

• Change the precondition such that we can call the method by passing both aliasing references and non-aliasing references to it as arguments without violating the precondition.

```
method alias(a: Ref, b: Ref)
 requires acc(a.f) && acc(b.f)
{
 a.f := 5b.f := 7assert a.f == 5
}
```

```
• Does the assertion still hold?
  Why (not)?
```
Challenges revisited

Heap data structures pose three major challenges for sequential verification

- Reasoning about aliasing
	- Permissions and separating conjunction

■ Writing specifications that preserve information hiding

And additional challenges for concurrent programs, e.g., data races

Field access: proof rules with permissions

Field read \mathcal{L}_max and \mathcal{L}_max and \mathcal{L}_max and \mathcal{L}_max and \mathcal{L}_max and \mathcal{L}_max and \mathcal{L}_max { **acc**(E.f) * P[x / E.f] } x := E.f { **acc**(E.f) * P } Field update \mathcal{L}_max and \mathcal{L}_max and \mathcal{L}_max and \mathcal{L}_max and \mathcal{L}_max and \mathcal{L}_max and \mathcal{L}_max { **acc**(x.f) * x.f == N } x.f := E { **acc**(x.f) * x.f == E[x.f / N] }

- Each field access requires (and preserves) the corresponding permission
- Permission to a location implies that the receiver is non-null
- Substitution with logical variable N in the field-update rule is needed to handle occurrences of x.f inside E (e.g., x.f := x.f + 1)

Framing

Frame rule { P } S { Q } { P ∧ R } S { Q ∧ R }

where S does not assign to a variable that is free in R

Unsound if S assigns to heap locations constrained by R

Framing

where S does not assign to a variable that is free in R

- The frame R must be self-framing
	- If heap locations constrained by R are disjoint from those modified by S , R is preserved
	- Otherwise, the precondition is equivalent to false (the triple holds trivially)
- § Example

{ $\mathsf{acc}(x.f) * x.f = N$ } $x.f := 5$ { $\mathsf{acc}(x.f) * x.f = 5$ }

 $\{acc(x.f) * x.f = N * acc(y.f) * y.f = 7\} x.f := 5 \{acc(x.f) * x.f = 5 * acc(y.f) * y.f = 7\}$

Framing (cont'd)

§ The following proof derives an incorrect triple. Why is it not a valid proof?

$$
\{ \; \mathsf{acc}(x.f) * x.f = N \; \} \; \; x.f := 5 \; \{ \; \mathsf{acc}(x.f) * x.f = 5 \; \}
$$

$$
\{ \; \mathsf{acc}(x.f) * x.f = N * x.f = 1 \; \} \; \; x.f := 5 \; \{ \; \mathsf{acc}(x.f) * x.f = 5 * x.f = 1 \; \}
$$

- Recall that the frame must be self-framing, which is not the case here
- § Making the frame self-framing yields a valid (but vacuous) proof

{ $\mathsf{acc}(x.f) * x.f = N$ } $x.f := 5$ { $\mathsf{acc}(x.f) * x.f = 5$ } $\{acc(x,f) * x.f = N * acc(x,f) * x.f = 1\} x.f := 5 \{acc(x,f) * x.f = 5 * acc(x,f) * x.f = 1\}$

Framing for method calls

```
method set(p: Ref, v: Int)
  requires acc(p.f)
  ensures acc(p.f) && p.f == v
{
 p.f := v}
```

```
// assume we have acc(x.f) 
   && acc(y.f)
set(x, 5)

assert x.f == 5
5 && y.f == 7assume y.f == 7
```

$$
\frac{\{\texttt{acc}(p,f)\}\text{ method set}(p,\ v)\ \{\texttt{acc}(p,f)*p,f=v\}}{\{\texttt{acc}(x,f)*\texttt{acc}(y,f)*y,f=7\}\ \texttt{set}(x,\ 5)\ \{\texttt{acc}(x,f)*x,f=5\}\}}
$$

- Frame rule enables framing without modifies clauses
- § A method may modify only heap locations to which it has permission

Permission transfer for method calls

- Permissions are held by method executions or loop iterations
- Calling a method transfers permissions from the caller to the callee (according to the method precondition)
- Returning from a method transfers permissions from the callee to the caller (according to the method postcondition)
- Residual permissions are framed around the call

Framing for loops

```
// assume we have acc(x.f) 
&& acc(y.f)
x.f := 0
x.f while (x.f < 10)
  invariant acc(x.f)
\{x.f := x.f + 1}
y.f := 7assert y.f == 7
```

$$
\frac{\{\texttt{acc}(x.f)*x.f < 10\} \ x.f:=x.f + 1 \ {\texttt{acc}(x.f)}\}}{\{\texttt{acc}(x.f)*\texttt{acc}(y.f)*y.f = 7\} \ \text{while}(x.f < 10) \ {\dots\} \ {\texttt{acc}(x.f)*\neg x.f < 10\}}}
$$

Permission transfer for loops

- **Permissions are held by method executions or loop iterations**
- Entering a loop transfers permissions from the enclosing context to the loop (according to the loop invariant)
- Leaving a loop transfers permissions from the loop to the enclosing context (according to the loop invariant)
- Residual permissions are framed around the loop

Permission transfer: inhale and exhale operations

- § **inhale** P means:
	- obtain all permissions required by assertion P
	- assume all logical constraints

- § **exhale** P means:
	- assert all logical constraints
	- check and remove all permissions required by assertion P
	- havoc any locations to which all permission is lost

Encoding of method bodies and calls

```
method foo() returns (…)
  requires P
  ensures Q
{ S }
```
 $x := foo()$

■ Encoding with heap

■ Encoding without heap and globals

§ **inhale** and **exhale** are permission-aware analogues of **assume** and **assert**

Exercise: definition of exhale

- § **exhale** P means:
	- assert all logical constraints
	- check and remove all permissions required by P
	- havoc (reset) any locations to which all permission is lost
- Write an example that demonstrates that omitting the havoc from the exhale encoding would be unsound

Encoding of loops

■ Reminder: encoding without heap

```
assert I
havoc targets
assume I
if(*) {
  assume b
 // encoding of S
  assert I
  assume false
} else {
  assume !b
}
```
■ Encoding with heap

```
exhale I
havoc targets
inhale I
if(*) {
  assume b
 // encoding of S
  exhale I
  assume false
} else {
  assume !b
}
```
Encoding of allocation

• new-expression specifies the relevant fields

 $x := new(f, g)$

■ Encoding chooses an arbitrary reference and inhales permissions to relevant fields

```
var x: Ref
inhale acc(x.f) && acc(x.g)
```
■ Incomplete information about freshness of new object

$$
x := new(f)
$$
\n
$$
y := new(f)
$$
\nassert x != y

Exercise: working with permissions

- **Implement, specify, and verify a class for** bank accounts with the following methods:
	- create returns a fresh account with initial balance 0
	- deposit deposits a non-negative amount to an account
	- transfer transfers a non-negative amount between two accounts
	- Account balances are integers.

• Verify the client program on the right.

\rightarrow 07-account.vpr

Verifying memory safety

- Memory safety is the absence of errors related to memory accesses, such as, null-pointer dereferencing, access to un-allocated memory, dangling pointers, outof-bounds accesses, double free, etc.
- Using permissions, Viper verifies memory safety by default

Challenges revisited

Heap data structures pose three major challenges for sequential verification

- Reasoning about aliasing
	- Permissions and separating conjunction
- Framing, especially for dynamic data structures
	- Sound frame rule, but no support yet for unbounded data structures

■ Writing specifications that preserve information hiding

And additional challenges for concurrent programs, e.g., data races

Objects and the heap

- 1. Heap model
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Heaps

■ Encode references and fields

■ Heaps map references and field names to values

type HeapType = **Map**<T>[(Ref, Field T), T] *// polymorphic map*

■ Represent the program heap as one global variable

var Heap: HeapType

Permissions and field access

■ Permissions are tracked in a global permission mask

```
type MaskType = Map<T>[(Ref, Field T), bool]
var Mask: MaskType
```
- Gonvention: $-Mask[null, f]$ for all fields f
- Field access

$$
x.f := E
$$
\nassert Mask[x,f]

\nHeap[x,f] := E

- Field access requires permission!

Inhale

- § **inhale** P means:
	- obtain all permissions required by assertion P
	- assume all logical constraints
- Encoding is defined recursively over the structure of P

■ The encoding also asserts that E is well-defined (omitted here)

Exhale (1st attempt)

- § **exhale** P means:
	- assert all logical constraints
	- check and remove all permissions required by assertion P
	- havoc any locations to which all permission is lost
- Encoding is defined recursively over the structure of P

■ The encoding also asserts that E is well-defined (omitted here)

Example

inhale $acc(x.f)$ && $x.f == 5$

assume ¬Mask[x,f] Mask[x,f] := **true**

assert Mask[x,f] *// well-definedness check* **assume** Heap[x,f] == 5

exhale acc(x.f) && x.f == 5

assert Mask[x,f] Mask[x,f] := **false havoc** Heap[x,f] **assert** Mask[x,f] *// well-definedness check* **assert** Heap $[x, f]$ == 5

Exhale (fixed)

- Conceptually, permissions should be removed after checking logical constraints
- Adapt encoding
	- Check well-definedness against mask at the beginning of the exhale
	- Delay havoc until the end of the exhale

```
exhale P
```

```
var oldMask: MaskType
var newHeap: HeapType
oldMask := Mask
[[exhale P]] // like before, but no havoc and with 
                    well-definedness check on oldMask
assume forall y,g :: Mask[y,g] ==> newHeap[y,g] == Heap[y,g]
Heap := newHeap // effectively havocs all locations to which 
                    permission was lost
```
Exercise: encoding of exhale

■ Encode the operation

```
exhale acc(x.f) && x.f == 5
```
with the fixed encoding.

Challenges revisited

Heap data structures pose three major challenges for sequential verification

- Reasoning about aliasing
	- Permissions and separating conjunction
- Framing, especially for dynamic data structures
	- Sound frame rule, but no support yet for unbounded data structures
- Writing specifications that preserve information hiding
	- Not solved, but see next module

And additional challenges for concurrent programs, e.g., data races

- Permissions are an excellent basis, but see later

